

A Verified Foreign Function Interface between Coq and C

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One can write dependently typed functional programs in Coq, and prove them correct in Coq; one can write low-level programs in C, and prove them correct with a C verification tool. We demonstrate how to write programs partly in Coq and partly in C, and interface the proofs together. The Verified Foreign Function Interface (VeriFFI) guarantees type safety and correctness of the combined program. It works by translating Coq function types (and constructor types) along with Coq functional models into VST function-specifications; if the user can prove in VST that the C functions satisfy those specs, then the C functions behave according to the user-specified functional models (even though the C implementation might be very different) and the proofs of Coq functions that call the C code can rely on that behavior. To achieve this translation, we employ a novel, hybrid deep/shallow description of Coq dependent types.

CCS Concepts: • **Software and its engineering** → **Software verification**; **Interoperability**; **Formal software verification**.

Additional Key Words and Phrases: foreign function interface, Coq, C

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1 Introduction

We want to write functional programs, because proving those correct is simpler than proving imperative pointer programs. After we prove our programs correct, we want to compile and run them. One can prove programs using Coq, whose logic contains a pure functional programming language along with the proof theory for proving that those programs satisfy logical specifications. Then one can “extract” the programs to OCaml, and compile and run them. But the OCaml compiler (written in OCaml) is not proved correct; nor is the OCaml runtime system and garbage collector (written in C). We want *foundational* verification, in which the application program and all these tools can be proved correct in the same machine-checked logic, in theorems that compose together to make a single end-to-end correctness theorem.

For proved-correct compilation, one can use CertiCoq, a compiler from Coq to C that is verified in Coq. It composes with the CompCert verified C compiler and the CertiGC verified garbage

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collector (see [section 2](#)). Thus, a verified functional program in Coq compiled and executed with CertiCoq+CompCert+CertiGC can have the desired end-to-end correctness theorem in Coq.¹

However, large programs are rarely written in a single language; additional languages are used for better performance or for capabilities that the primary language lacks. In particular, because Coq lacks primitive types,² mutation, and input/output actions, CertiCoq-compiled code must interact with another language to have those capabilities. Specifically (for the CertiCoq back-end targeting C), Coq code must be able to call C code and C code must be able to inspect and generate Coq data structures and call Coq code. There are already *foreign function interface* (FFI) systems to handle the *operational* interface between functional languages (ML, Haskell, etc.) and C [[Blume 2001](#); [Leroy 1999](#)], or Java-like languages and C [[Liang 1999](#)]. Some of these provide APIs for the functional language to traverse C data structures, others provide APIs for C to traverse the functional language’s data structures; and all provide APIs for the functional language to call C functions. In these systems, a type-directed “glue code generator” produces APIs and interface functions. Those FFIs make a *dynamic* (operational) connection between the high-level and low-level language; and some work has even addressed type safety [[Tan et al. 2006](#)].

But previous work has not addressed dependently typed high-level languages, and most importantly, has not shown how to connect *correctness proofs* of high-level client programs with correctness proofs of low-level primitives. When we prove a functional program correct in Coq’s proof theory (the Calculus of Inductive Constructions) and we prove a C program correct in a program logic for C, how does the “glue code” work to connect these proofs together?

We provide a solution to that problem: **VeriFFI**, a **Verified Foreign Function Interface** between Coq and C ([Figure 1](#)). Coq program components are proved correct directly in Coq, C program components are locally proved correct using the Verified Software Toolchain (VST) [[Appel et al. 2014](#)], and the connection is made via VST function specifications that are generated by VeriFFI.

Compared to some other verified FFI systems (in [section 14](#) we discuss related work), it’s important that our high-level language is a higher-order dependently typed pure functional language embedded in a logic (i.e., Coq). “Functional” programming languages with mutation (such as OCaml) require separation logic for their reasoning on both sides of the FFI [[Meijer 2014](#)]; our approach limits separation logic only to the C side. And (unlike other verified FFI systems) our C language verification can be done using a powerful and general proof tool, the Verified Software Toolchain.

Contributions

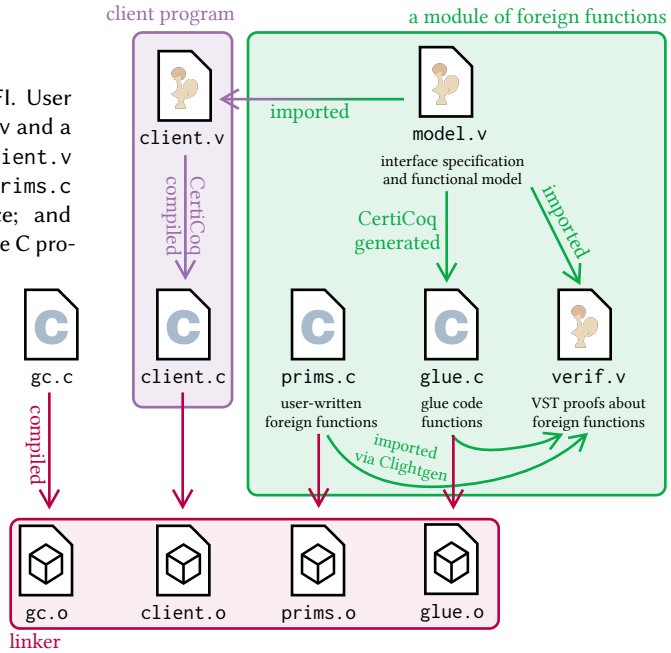
- VeriFFI guarantees both type safety and correctness (except for termination) of the foreign functions, and supports both data abstraction (C functions on types that are opaque to the Coq side) and data transparency (C functions on Coq inductive types).
- We achieve this by calculating C function specifications (pre/postconditions) from Coq dependent types; the user can use VST to prove that the C functions satisfy these specs.
- We calculate these specs using a novel hybrid deep/shallow description of Coq types that allows annotation on each component of a type; the annotations allow analysis and translation of Coq’s dependent type structure for this and other applications in metaprogramming.
- Our semantic approach and our glue code generators provide language-local reasoning on the Coq side and the C side without the need for a multi-language semantics.

¹Each of these components is verified in Coq to specifications that are consistent with each other, but CertiCoq’s composed end-to-end correctness theorem has not yet been demonstrated. In fact, our work in this paper informs the statement of that theorem; see [section 13](#).

²Or, to the extent that Coq supports primitive types such as 63-bit integers, the correctness of their implementation can be proved by considering their operations as foreign functions.

Fig. 1. Typical usage of VeriFFI. User writes an interface spec `model.v` and a proved-correct client program `client.v` in Coq; writes a C program `prims.c` that implements the interface; and proves in `verif.v` in Coq that the C program is correct.

(Clightgen is CompCert’s front end that parses C into a Clight AST, to be verifiable by VST)



2 Background

*CertiCoq*³ compiles Coq functions by first reifying them into ASTs using MetaCoq [Sozeau et al. 2019], then translating to an untyped intermediate language λ ANF [Paraskevopoulou et al. 2021] and then to CompCert Clight, a high-level intermediate language of the CompCert verified C compiler [Leroy 2006]. From there, CompCert can compile to assembly language. Each of these languages—(reified) Coq, λ ANF, Clight, Assembly—has a formal operational semantics in Coq. Coq’s formalization is part of MetaCoq, λ ANF’s is part of CertiCoq’s proof, and Clight’s and Assembly’s are part of the CompCert specification. Each of the translations (as well as each optimization pass from λ ANF to λ ANF) is proved correct (semantics-refining) with machine-checked proofs in Coq, with respect to the respective operational semantics.

The first phase of CompCert translates C to Clight. Clight programs are readable as C programs—Clight can be translated to C with an unverified pretty-printer, when it is useful to compile the output of CertiCoq with an unverified C compiler such as `clang` or `gcc`. Hence we will treat C and Clight as mostly interchangeable.

CertiCoq had a mechanism for external primitive functions written in C, but had no mechanism for verifying them. CertiCoq’s correctness proof is w.r.t. the Clight operational semantics, but for program verification (of external C functions) one might want an axiomatic semantics, a program logic. And there was the additional challenge of reasoning about shared structure in a garbage-collected heap, and preserving invariants across garbage collections.

The Verified Software Toolchain (VST) [Appel et al. 2014] is a program logic and tool for proving functional correctness of Clight programs, and of C programs via their translation to Clight. Clight

³There is no single citable work that describes all of CertiCoq. Separate papers describe different parts of the compiler and runtime: • the workshop paper announcing the beginning of the project [Anand et al. 2017] • CertiCoq’s front end is MetaCoq via PCUIC [Sozeau et al. 2019] • the verified translation from MetaCoq to its λ ANF intermediate language [Paraskevopoulou and Grover 2021] • the verified shrink-reduction optimization phase [Savary Bélanger and Appel 2017] • the verified closure-conversion pass [Paraskevopoulou and Appel 2019] • the composition of all λ ANF phase verifications [Paraskevopoulou 2020] • the verified code generator [Savary Bélanger et al. 2019] • the CertiGC verified garbage collector [Wang et al. 2019].

is an easier language than C for program verification as it has no side effects inside expressions. VST has a formal soundness proof in Coq—that is, if you prove a property of a C program in VST, then that program running in the operational semantics of Clight will respect that property.

VST is used for the correctness proof of CertiCoq’s garbage collector [Wang et al. 2019], which is written in C. The Clight code produced by CertiCoq allocates records (from the compilation of inductive data constructors) on a garbage-collected heap, and from time to time it must call the garbage collector (g.c.).

The proof of a C function in VST is with respect to a *function specification* (funspec), that gives the function precondition and function postcondition, all in higher-order impredicative separation logic, and all with respect to a set of quantified variables \vec{x} : if the program state before calling f satisfies $\text{pre}(\vec{x})$ and if f terminates (in the Clight operational semantics), then the program state will satisfy $\text{post}(\vec{x})$.

Combining Coq and C. Now, suppose a Coq function g calls a C function f ; or more precisely, a Coq function g translated to a Clight function g_c calls a Clight function f . From the MetaCoq semantics of g and a CertiCoq correctness theorem for open programs as proposed in section 13, one would get a Coq proof about the behavior of g_c (subject to an assumption about f ’s behavior) in Clight operational semantics. Given some appropriate funspec for f in VST’s logic, the user can interact with VST to prove correctness of f w.r.t. that funspec. Based on the semantic model of VST funspecs, that gives a Coq proof about the behavior of f in Clight’s operational semantics.

VeriFFI’s job will be to say what that funspec should be, and to provide the appropriate definitions and tools to make this connection. With VeriFFI, the foreign C function could be the garbage collector, a user-written C function, or a VeriFFI glue-code-generated C function. Any of these functions manipulate C data structures that are the CertiCoq translations of Coq data structures, as well as other C data structures that the C functions use internally. An important part of VeriFFI’s job is to enable both concrete data types (C traversal and construction of Coq Inductive types) and abstract data types (whose representation is not known to the Coq client).

Data representations. CertiCoq represents Coq values in memory using the same low-level memory representations as OCaml [Minsky and Madhavapeddy 2022].⁴ In this discussion, we assume a 64-bit word size. Unsigned integers n up to $2^{63} - 1$ are represented in memory as $2n + 1$. Since all pointers are word-aligned (and thus even numbers), this allows the garbage collector to distinguish pointers from nonpointers.

Inductive `nat := 0 : nat | S : nat -> nat.`

Inductive types such as `nat` are represented as follows. The `0` constructor, as the first constant constructor in this datatype, is represented by an *unboxed* (i.e., tagged as nonpointer) zero, $2 \cdot 0 + 1$. The value `S n` is represented by a *aligned* (even) pointer into a two-word record, where the *header* (at offset -1) contains a *length* (in this case, 1) and a *tag* (in this case 0, for the first *boxed* constructor).



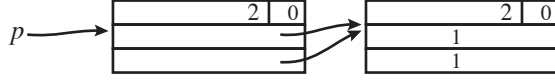
The Coq heap in separation logic. We must describe Coq values in their C representations, using VST’s separation logic. Trees in separation logic are typically represented as the separated conjunction of their subtrees, but that can’t work for the usual implementation of an ML-like functional

⁴There is no need to use OCaml representations, since we do not link with an OCaml system, but we maintain compatibility because it may be useful in the future.

language. Consider a program with shared subtrees:

```
Inductive tree := leaf : tree | node: tree -> tree -> tree.
```

```
let x := node leaf leaf in
let y := x in
let p := node x y in ...
```



Because there is sharing between x and y , we cannot describe this in separation logic as $p \mapsto \text{node } x \ y * x \mapsto \text{node leaf leaf} * y \mapsto \text{node leaf leaf}$.

We handle graph structures with sharing using the CertiGraph library [Wang et al. 2019], whose approach is to describe a graph g in the “propositional” part of Coq, as a mapping from vertex-numbers to edge-lists (and other information). It is a *labeled* graph, where each vertex-label includes the C address of the record representing that vertex (or, for vertices represented unboxed, the vertex-label has the unboxed value). Then the separation-logic resource (`graph_rep g`) describing this graph is the iterated separating conjunction (big-star) of all of its vertices.

CertiCoq uses a generational garbage collector, proved correct using VST [Wang et al. 2019]. That collector, or any collector, will need a *heap-management data structure* to keep track of memory not currently allocated but available for allocation.

In the VST proof of a C program that interacts with the CertiCoq garbage-collected heap, the separation-logic assertions will usually have these (separated) conjuncts: **heap**, described by the `graph_rep` predicate; (separated from) **thread_info predicate** comprising the heap-management data-structure and the stack of frames (a data structure keeping track of local variables pointing into the heap, following McCreight et al. [2010]) in the function-call stack.⁵

3 VeriFFI in a nutshell

Foreign functions are useful when the C code can use better data structures than Coq’s **Inductives**, or can use mutable data structures, or can access special machine instructions such as cryptographic primitives; or when the program needs to do I/O. We illustrate how to write such programs with VeriFFI using a simple example: 63-bit unsigned integers as a foreign type, with foreign functions to add (modulo 2^{63}) and convert from/to Coq’s natural number type. We use 63-bit integers to leave space for the 1-bit tag that marks unboxed values for the garbage collector.

3.1 Operational

A typical use of VeriFFI is structured as shown in Figure 1. Coq file `model.v` specifies an interface (Coq inductive types, foreign abstract types, and foreign functions with their Coq functional models). Coq file `client.v` has a program that uses the foreign functions. Figure 2 shows an example that uses a C implementation of 63-bit unsigned integers. On the Coq side (Figure 2a, `model.v`), we define an API as a Coq module type `UInt63`, then make the claims in `Module C` that there are instantiations of type `C.t` and functions `C.from_nat`, `C.to_nat`, and `C.add`. The client can use this API in writing Coq functions (Figure 2b, `client.v`).

Coq’s execution compiles the files `model.v` and `client.v` via the CertiCoq compiler, producing:

```
glue.c containing glue code for construction and traversal of Inductives used by the API;
client.c the compilation of the client program.
```

⁵There is one more separated conjunct: **outliers**, data structures outside the garbage-collected heap, to which the heap may point. These are not essential to the presentation in this paper and we will omit further mention of them.

```

Module Type UInt63.
  Parameter t : Type.
  Parameter from_nat : nat -> t.
  Parameter to_nat : t -> nat.
  Parameter add : t -> t -> t.
End UInt63.

Module C : UInt63.
  Axiom t : Type.
  Axiom from_nat : nat -> t.
  Axiom to_nat : t -> nat.
  Axiom add : t -> t -> t.
End C.

CertiCoq Register [
  C.from_nat => "uint63_from_nat",
  C.to_nat => "uint63_to_nat",
  C.add => "uint63_add"
] Include [ "prims.h" ].
CertiCoq Generate Glue
  -file "glue" [ nat ].
      (a) Coq side, model.v

Definition prog :=
  C.to_nat (C.add (C.from_nat 1)
               (C.from_nat 2)).

CertiCoq Compile
  -file "client" prog.
      (b) Coq side, client.v

value uint63_from_nat(
  struct thread_info *tinfo,
  value n) {
  value temp = n;
  uint64 i = 0;
  while (get_nat_tag(temp) == S) {
    i++; temp = get_args(temp)[0];
  }
  return (value) ((i << 1) + 1);
}

value uint63_to_nat (
  struct thread_info *tinfo,
  value t) {
  uint64 i = ((uint64)t)>>(uint64)1;
  value temp = make_nat_0();
  while (i) {
    if (tinfo->limit - tinfo->alloc < 2) {
      value roots[1]={temp};
      struct stack_frame fr =
        {roots+1,roots,tinfo->fp};
      tinfo->fp= &fr;
      tinfo->nalloc = 2;
      garbage_collect(tinfo);
      temp=roots[0]; tinfo->fp=fr.prev;
    }
    temp = alloc_make_nat_S(tinfo, temp);
    i--;
  }
  return temp;
}

value uint63_add(
  struct thread_info *tinfo,
  value x, value y) {
  return (value) ((uint64)x+(uint64)y-1);
}
      (c) C side, prims.c

```

Fig. 2. Operational View of the FFI: Code in Coq (left) vs code in C (right).

These components link at C level, with the garbage collector (gc.c) and with user-written prims.c (Figure 2c) which instantiates the axioms in Module C. The C foreign functions have this API:

```

/* prims.h */
#include <gc.h>
value uint63_from_nat(struct thread_info *tinfo, value z);
value uint63_to_nat(struct thread_info *tinfo, value t);
value uint63_add(struct thread_info *tinfo, value x, value y);

```

Each function's first parameter is a thread-info pointer, needed in case the function allocates on the heap. The remaining arguments correspond to the Coq arguments of the (uncurried) Coq function type. Each of these may be a concrete Coq type (such as `nat`) or an abstract Coq type (such as `C.t`). Either way, the C parameter type is just `value`, which is a typedef for `void*`.

The `thread_info` parameter describes (among other things) the location of the next allocable spot in the heap (`tinfo->alloc`); the end of the allocation space (`tinfo->limit`); and other data structures used only by the garbage collector. If `limit` minus `alloc` is less than the size of a new record (including header), then `garbage_collect` must be called.

All the operations on `C.t` are foreign functions—it is an abstract data type—so we are free to choose an efficient representation. Here, we implement `C.t` using C’s unsigned 64-bit integers, and we represent `nat` as shown in [section 2](#). The functions in `prims.c` are implemented as follows:

uint63_from_nat: To convert the low-level memory representation of `nat` to C’s native 64-bit integer type, we have to count the number of `S` constructors in the data structure. The function getting the tag and the one accessing the arguments are *glue functions*, generated automatically in `glue.c`.

uint63_to_nat: uses the (automatically generated) glue function `alloc_make_nat_S` to allocate a *successor* constructor on the heap, as many times as called for by the input argument `t` (after its low-order tag bit is stripped off). It is a precondition of `alloc_make_nat_S` that enough space is available; to provably satisfy this precondition, we first test `limit - alloc`. In case a garbage collection is needed, the local variable `temp` is a *root* of the heap, so we need to push a frame on the stack of frames and copy `temp` into that frame; then after the collection, copy back the (possibly forwarded) `temp` and pop the stack.

add: To add two tagged integers (modulo 2^{63}), first shift each right to strip the tag; then add; then shift left and add 1. Or do it more efficiently, as shown.

3.2 Verification

Previous FFI systems have been able to “glue” at the operational level as described in [subsection 3.1](#); but VeriFFI can connect specifications and proofs. We start by providing a *functional model* of (in this example) the `UInt63` module type:

Module `FM` <: `UInt63`.

Definition `t` : Type := {z : nat | z < 2 ^ 63}.

Lemma `mod63_ok`: forall (n : nat), (n mod (2^63) < 2^63).

Proof. **intro**. **apply** `Nat.mod_upper_bound`, `Nat.pow_nonzero`. **auto**. **Qed**.

Definition `from_nat` (n : nat) : t := (n mod (2^63); mod63_ok _).

Definition `to_nat` (z : t) : nat := let '(n; _) := z in n.

Definition `add` (x y : t) : t :=

let '(xn; x_pf) := x in let '(yn; y_pf) := y in ((xn + yn) mod (2^63); mod63_ok _).

End `FM`.

We model a 63-bit integer as a natural number n accompanied by a proof that $n < 2^{63}$. Then our definition of `to_nat` is trivial (just project out n), but in the definitions of `from_nat` and `add` we must supply a proof that the result is in range, which we do using an auxiliary lemma `mod63_ok`. You can see in the functional model that the behavior of `from_nat` and `add` forces the results to be in range by explicitly doing a modulo operation, which models unsigned integer overflow.

VeriFFI guarantees that `C.t` and `FM.t` are isomorphic and that the operations (such as `add`) respect this isomorphism—provided that the user proves certain things about the C program as specified below. This is sufficient to prove the correctness of the client program. For example, we can prove that the `prog` in [Figure 2](#) computes the number 3, or that `add` is associative.

In the next five sections, we will show how VeriFFI represents the reified types of foreign functions and Coq inductive constructors; how (based on these and on user-supplied functional models) VeriFFI generates VST funspecs that serve as theorem statements that the user must prove about the C program implementations. Then in [section 9](#) we complete the `UInt63` example:

- the funspec computed for `uint63_to_nat`;

- the proof that `uint63_to_nat` satisfies this funspec; and
- the functional correctness proof of the client program, relying on the fact that the foreign functions satisfy their specs.

4 Graph predicates synthesized from descriptions of dependent types

To make a *verified* FFI that connects proofs across the interface, we need a specification framework relating Coq data structures to heap-graph vertices. For each Coq inductive type, we must describe (parametrically) how each data constructor is represented as graph edges emanating from a graph vertex. To do that, we use the notion of a *graph predicate*, bundled with its invariants into a Coq type class:

```
Class InGraph (A : Type) : Type :=
{ graph_predicate : graph -> outlier_t -> A -> rep_type -> Prop
; has_v : ... (* CertiGraph-related property of graph_predicate *)
; is_monotone : ... (* graph_predicate preserved under heap allocation *)
; gc_preserved : ... (* graph_predicate preserved under g.c.-isomorphism *)
}.
```

A `rep_type` is a graph vertex, corresponding to the address of a boxed value (represented as an aligned pointer, last bit 0) or an unboxed integer (represented as $2n + 1$, last bit 1). That is, `graph_predicate g x p` says that value `x` of type `A` is represented at vertex `p` in graph `g`.

Of course, each different Coq type `A` has its own different data representations; hence `graph_predicate` is not a single fixed predicate, it is a Coq type class indexed by type `A`. The VeriFFI system automatically constructs instances of this type class, and proves automatically (for each instance) that `graph_predicate` satisfies the properties specified in the `InGraph` type class.

For example, consider the inductive type `vec`, polymorphic lists indexed by length:

```
Inductive vec (A : Type) : nat -> Type :=
| vnil : vec A 0
| vcons : forall n, A -> vec A n -> vec A (S n).
```

The (type-indexed) graph predicate for this type is,

```
Instance InGraph_vec (A : Type) (InGraph_A : InGraph A) (n : nat) : InGraph (vec A n) :=
  let fix graph_predicate_vec (n : nat) (g : graph)
      (x : vec A n) (p : rep_type) {struct x} : Prop :=
    match x with
    | vnil => match p with repZ z => z = 0 | _ => False end
    | vcons arg0 arg1 arg2 =>
      exists p0 p1 p2 : rep_type,
        @graph_predicate nat InGraph_nat g arg0 p0 /\
        @graph_predicate A InGraph_A g arg1 p1 /\
        graph_predicate_vec arg0 g arg2 p2 /\
        match p with
        | repNode v => compatible g v 0 (raw_fields v) [p0; p1; p2] /\
          raw_mark v = false /\ raw_color v = 0 /\ raw_tag v = 0
        | _ => False
        end
    end in { | graph_predicate := (graph_predicate_vec n); has_v := ...; ... | }.
```

One can see that `vnil` is represented by a *constant* ($z=0$), and `vcons n h t` is represented as vertex `p` in graph `g`, such that `p` has three out-edges to vertices `[p0; p1; p2]` (ensured by the `compatible` predicate), and those also have (type-class-indexed) graph predicates. Importantly, the conjunctions are ordinary, not separating, which permits overlap between the graph structures of `p0, p1, p2`.

Building such instances is cumbersome and technical, whether or not they involve dependent types. To build such instances automatically, we implemented generators using MetaCoq. These generators inspect a particular inductive data type, identify the other inductive types used in that type, infer the `InGraph` instances for those types, generate them if they are missing, and prove the required lemmas about it via Ltac. (In the actual implementation, `InGraph` is split into two type classes: `graph_predicate` is in a separate type class from the lemmas to make it easier to automatically prove the lemmas for each instance.)

5 Reified descriptions with annotations

Graph predicates are the basic building blocks of the function specifications of generated glue code and foreign functions. We want to generate these function specifications automatically, but generating VST specifications *directly* from MetaCoq would be difficult. MetaCoq operates on the core language of Coq, and focuses on metatheory rather than easy code generation. The notation-heavy style of VST specifications also make it challenging to generate them from a fully deeply embedded description.

To get around these problems, we introduce an intermediate representation between MetaCoq and function specifications, tailored to the information we require to state a function specification – a *reified description*. We will use metaprogramming to obtain MetaCoq’s representation of inductive types and constructors to convert them into our representation; then we can generate the specifications we need from our intermediate representation, in pure Gallina. This isolates metaprogramming to the first half of this conversion and simplifies the specification generation later.

This reified description is defined as:

```
Inductive reified (ann : Type -> Type) : Type :=
| TYPEPARAM : (forall (A : Type) `(ann A), reified ann) -> reified ann
| ARG : forall (A : Type) `(ann A), (A -> reified ann) -> reified ann
| RES : forall (A : Type) `(ann A), reified ann.
```

Our description type is parametrized by `ann`, an annotation type class, whose important instances will be *constructor annotation* and *foreign function annotation* (see [section 6](#) and [subsection 8.1](#)). Thanks to `ann`, reified descriptions can carry extra information related to every component of the described type. The reified description type consists of 3 constructors:

- The `TYPEPARAM` constructor represents type parameters of a function or a constructor. It takes a higher-order function as an argument, where the function takes a Coq type `A` as an argument, along with a guarantee that there is an instance of the `ann` type class, and returns another `reified` description. This way the rest of the description has access to the type parameter and its annotation instance in the context.
- The `ARG` constructor represents dependent arguments of a function or a constructor. `ARG` takes the type of the argument, a witness that there is a type class instance for that type, and finally a higher-order function that takes an argument and returns a `reified` description. This argument allows us to express dependently typed arguments since the argument of the higher-order function can occur in the rest of the description.
- Finally, the `RES` constructor represents the result type of a function. `RES` takes the result type and a witness that there is an annotation instance for that type.

Our representation combines both *deep embedding* and *shallow embedding* techniques. The description that would solve our problems had to be traversable, therefore we defined it as an inductive type, like a deep embedding. In the arguments of each constructor, however, we see the Coq semantics of the respective concept: for a type parameter, we have a function that takes a

type parameter, for an argument we have a function that takes an argument, resembling a shallow embedding.

This approach can be considered a special case of McBride [2010] or Prinz et al. [2022], except both object and host languages are Coq in our approach. This coincidence enables us to reuse more features of the host language than solely name binding; we can also annotate the components of a Coq type with Coq type class instances, we can interpret a Coq type description back to its corresponding Coq type without extra use of metaprogramming. This allows us to carry values satisfying a type description in a type-safe way, which we use in section 6 and subsection 8.1 to achieve reflection of constructors and foreign functions from their descriptions.

Using the `reified` type, we can now describe types of functions or constructors. For example, recall the `vec` type of section 4; its constructors `vnil` and `vcons` are described as:

```
(* vnil : forall (A: Type), vec A 0 *)
Definition vnil_reified : reified InGraph :=
  TYPEPARAM (fun (A : Type) (InGraph_A : InGraph A) =>
    RES (vec A 0) (InGraph_vec A InGraph_A 0)).

(* vcons : forall (A : Type) (n : nat) (x: A) (xs: vec A n), vec A (S n) *)
Definition vcons_reified : reified InGraph :=
  TYPEPARAM (fun (A : Type) (InGraph_A : InGraph A) =>
    ARG nat InGraph_nat (fun (n : nat) =>
      ARG A InGraph_A (fun (x : A) =>
        ARG (vec A n) (InGraph_vec A InGraph_A n) (fun (xs : vec A n) =>
          RES (vec A (S n)) (InGraph_vec A InGraph_A (S n))))))).
```

Not only inductive constructor types, but dependently typed foreign function types are described by `reified`. For example, the (non-foreign) function `length : forall {A : Type}, list A -> nat` can be described as:

```
Definition length_desc : reified InGraph :=
  TYPEPARAM (fun (A : Type) {InGraph_A : InGraph A} =>
    ARG (list A) (InGraph_list A InGraph_A) (fun (_ : list A) =>
      RES nat InGraph_nat)).
```

Consuming reified descriptions. We have many useful functions on `reified` descriptions, such as the one that calculates a `graph_predicate`. Here we show a simpler one, that calculates the (uncurried) argument type of a function, as a nested dependent tuple of the types of all type parameters and arguments in the description:

```
Fixpoint args {cls : Type -> Type} (r : reified cls) : Type :=
  match r with
  | TYPEPARAM k => {A : Type & {H : cls A & args (k A H)}}
  | ARG A H k => {a : A & args (k a)}
  | RES _ _ => unit
  end.
```

When we need to write a function that needs to quantify over all the arguments that a function or a constructor takes, we can use `args` of a `reified` description to achieve that. For the description of the `length` function, this would calculate:

```
args length_desc = {A : Type & { _ : InGraph A & { _ : list A & unit }}}
```

We can also write a function that calculates the result type of a function, whose implementation is similar to `args`:

```
Fixpoint result{cls: Type->Type}(r: reified cls)(xs: args r): {A: Type & cls A} := ...
```

Now, using `args` and `result`, we can write a function that gives us a type that is as close as possible to the original function or constructor type. In other words, we want to reflect the type description to an actual Coq type:

```
Definition reflect {cls : Type -> Type} (r : reified cls) : Type :=
  forall (P : args r), projT1 (result r P).
```

The type we obtain from this function is an uncurried version of the type of `length`. A function of type `reflect length_desc` would take a nested dependent tuple of all the arguments (and the annotations for type parameters) and return the same result type. Here is how that function would be implemented, where the nested tuple is pattern-matched in the parameter to `fun`:

```
Definition length_uncurried : reflect length_desc :=
  fun '(A; (_, (l; tt))) => @length A l.
```

The `reflect` function provides a type-safe way for us to go from the description into the original function. This will allow proofs by reflection, ensuring that the function we have fits the description we were provided.

Curried vs. uncurried. We have chosen to calculate the uncurried type of a multi-argument Coq function because the interface to C (and similar low-level languages) is more efficient and natural with all arguments at once in the uncurried style. Another reason for this choice is that the uncurried function type includes the annotation arguments, which are useful (for example) in calculating the `graph_predicate` instance from the `reified` description of a type. In this section we have instantiated the `ann` parameters with `InGraph`, but in the next sections we explain annotations useful for constructor types and for function types.

6 Constructor specifications

To compose proofs of Coq programs that build and traverse data structures with proofs of C programs that build and traverse those same data structures, the VST separation logic function-specifications for construction and projection must be coherent with the Coq constructors. To accomplish that, we introduce a novel deep and shallow *constructor description*, derivable automatically from MetaCoq descriptions of inductive data types; and an interpretation of those constructor descriptions into VST function specifications.

Constructor descriptions. The glue code generator (section 7) builds C functions that construct Coq values, such as `alloc_make_vec_vcons`.

We calculate formal specifications of these functions in VST's specification language, from the `reified` description of the constructors. As usual, `reified` must be supplied with an appropriate annotation type. For data constructors, class `ctor_ann` contains the information we need:

```
VARIANT erasure := no_placeholder | has_placeholder | present.
Class ctor_ann (A : Type) : Type := {field_in_graph : InGraph A; is_erased : erasure}.
```

In section 4, we defined the `InGraph` type class, which consists of a graph predicate and lemmas about it for a given Coq type. The first field of the `ctor_ann` type class is an instance of `InGraph` for each field of the constructor we want to annotate. This allows us to specify how the values of the arguments are represented in the heap graph.

The second field, `is_erased`, tells us whether a constructor field is erased during compilation: In CertiCoq, *computationally irrelevant* values, such as values of type `Type` or values of kind `Prop`, are erased. When they are arguments to constructors or functions, their places are occupied by (unit) placeholders. Some values are entirely erased in the memory representation, such as parameters of inductive types.

Now that we have a `ctor_ann` type to annotate our `reified` descriptions with, VeriFFI defines a record that contains all the information we need about a constructor:

```
Record ctor_desc :=
  { ctor_name : string ; ctor_reified : reified ctor_ann
  ; ctor_reflected : reflect ctor_reified ; ctor_tag : nat ; ctor_arity : nat }.
```

Along with the name, tag, and arity of a constructor, we include the `reified` description of a constructor, in the `ctor_reified` field. Using dependently typed records, we include the field `ctor_reflected`, the `reflected` version of the `reified` description we just included in the record.

Here we can see some example `ctor_desc` values for the `vnil` and `vcons` constructors of the `vec` inductive type:

```
Definition vn timer_desc : ctor_desc :=
  { | ctor_name := "vnil"
    ; ctor_reified := . . . (* like vn timer_reified but with ctor_ann annotations *)
    ; ctor_reflected := fun '(A; (_, tt)) => @vn timer A
    ; ctor_tag := 0; ctor_arity := 0 |}.
```

```
Definition vcons_desc : ctor_desc :=
  { | ctor_name := "vcons"
    ; ctor_reified := . . . (* like vcons_reified but with ctor_ann annotations *)
    ; ctor_reflected := fun '(A; (_, (n; (x; (xs; tt)))) => @vcons A n x xs
    ; ctor_tag := 1; ctor_arity := 3 |}.
```

VeriFFI's glue code generator defines a type class that allows easy transition from the real Coq constructor for an inductive type, into the `ctor_desc` for that constructor; and we can define instances for every constructor we generate descriptions for:

```
Class Desc {T : Type} (ctor_val : T) := { desc : ctor_desc }.
Instance Desc_vn timer : Desc @vn timer := { | desc := vn timer_desc |}.
Instance Desc_vcons : Desc @vcons := { | desc := vcons_desc |}.
```

`Desc` does not come with a guarantee that the `reified` description matches the real Coq value. However, describing the wrong constructor in the `Desc` instance means the verification of the function specifications will fail later, so it can't lead to unsoundness.

Constructor descriptions are generated automatically; their generation is implemented mostly in `MetaCoq` and `Ltac`.

7 Operational glue code generation

CertiCoq Generate Glue generates C-language data-structure traversal and constructor functions for a user-specified set of Coq **Inductive** types:

```
CertiCoq Generate Glue [ vec , nat ].
```

For instance, for the `vec` type, VeriFFI generates these functions:

```
value make_vec_vn timer(void) { return (value) 1; }

value alloc_make_vec_vcons
  (struct thread_info *tinfo, value arg0, value arg1, value arg2) {
  value *argv = tinfo->alloc;
  argv[0] = (value) 3072; argv[1] = arg0; argv[2] = arg1; argv[3] = arg2;
  tinfo->alloc = tinfo->alloc + 4; return argv + 1;
}
```

Unboxed constructors, such as `vnil`, are represented as (odd) integers. Boxed constructors, such as the `vcons`, are represented as pointers to memory locations that store the constructor arguments. This memory can exist either within the `CertiCoq` runtime's garbage-collected memory region (the

CertiCoq heap) or as “outliers” in the *C heap*. The `alloc_make_vec_vcons` function uses the thread-info to find the next unused word of the g.c. allocation space `tinfo->alloc`. It is a precondition of this function that at least 4 words of space are available (for the header, the length index, the head, and the tail); prior to calling the function, this precondition may be tested by a quick comparison, or established (if that fails) by calling the garbage collector.

VeriFFI formally specifies and verifies the C code of these glue functions. For each glue code function, VeriFFI generates a VST funspec from the constructor description (`ctor_desc`), and then automatically produces a VST correctness proof. We will not show the details of glue-code funspecs, but we explain VST funspecs for foreign functions in [subsection 9.1](#).

Discriminating Coq constructors. For each Coq inductive type, VeriFFI generates a C function that allows the user to determine which Coq constructor had been used to create a given value. For example, for the `vec` type, the function would be:

```
size_t get_vec_tag(value v) {
  if (is_ptr(v)) /* that is, if v is an even number */
    switch (((size_t*)v)[-1]&255) { /* fetch header, mask out all but constructor tag */
      case 0: return 1; default: /* unreachable */;
    } /* there would be more cases if more boxed constructors than vcons */
  else switch (v >> 1) { /* strip off the tag bit */
    case 0: return 0; default: /* unreachable */;
  } /* there would be more cases if more unboxed constructors than vnil */
}
```

This function returns the *tag* of the constructor used to create this value, an index based on the order in which the Coq **Inductive** listed the constructor names.

Extracting arguments of a Coq constructor. Given a Coq value of an inductive type, to access its constructor arguments, we have a C function that works on values of any inductive boxed constructor:

```
value *get_args(value v) { /* this function can always be inlined */
  return (value *) v;
}
```

Effectively this casts a pointer into an array of values, so the arguments of an arity-*n* constructor can be accessed with `get_args(v)[0]`, ..., `get_args(v)[n-1]`.

Calling Coq closures. The CertiCoq compiler represents Coq functions as closures at runtime, which consist of a function-pointer and an environment-pointer. To call these from C, one must fetch the code-pointer, fetch the environment pointer, and pass the environment as one of the arguments to the code-pointer function. We have a C function that implements this protocol:

```
value call(struct thread_info *tinfo, value clo, value arg) {
  value f = ((struct closure *) clo)->func;
  value envi = ((struct closure *) clo)->env;
  return ((value (*)(struct thread_info *, value, value)) f) (tinfo, envi, arg);
}
```

8 Foreign function specifications

When proving correctness of a Coq program that calls functions implemented in C and proved correct in VST, the VST function specification must be coherent with an appropriate Coq functional model. In this chapter we show how to generate a coherent VST function specification from a reified function description. Coherence on the Coq side is assured by reflection. Coherence on the C side is assured by a Coq proof using VST’s program logic.

8.1 Foreign function descriptions

Foreign functions may use Coq inductive types and also user-defined foreign types such as 63-bit integers or packed strings that are not (efficiently) expressible in Coq inductive types. Since `reified` descriptions allow us to annotate every component of a function type, we can define an annotation type that contains additional information about the foreign types we may need to use.

A user of our system will define their foreign types and foreign functions as axioms in Coq. In [section 3](#) we showed axioms stating the existence of a C representation and operations on 63-bit unsigned integers; and the corresponding functional model FM:

```
Module C : UInt63.
  Axiom t : Type.
  Axiom from_nat : nat -> t.
  Axiom to_nat : t -> nat.
  Axiom add : t -> t -> t.
End C.

Module FM <: UInt63.
  Definition t : Type := {n : nat | n < 2^63}.
  Definition from_nat (n : nat) : t := ...
  Definition to_nat (x : t) : nat := ...
  Definition add (x y : t) : t := ...
End FM.
```

The `C` module contains Coq axioms for the foreign types and Coq axioms for foreign functions that may use these foreign types. These functions will be realized by `C` functions through the FFI. The user must justify all these axioms by defining a type `C.t` and Coq functions `C.from_nat` (etc.) such that an isomorphism between modules `C` and `FM` can be proved.

To connect the functional model to the `C` type in a `reified` description of a foreign function such as `add`, we provide an *annotation* to `reified`. For constructor descriptions we instantiate the `ann` parameter with `ctor_ann`, and for functions, with `foreign_ann`:

```
Class foreign_ann (model : Type) : Type :=
{ foreign : Type
; foreign_in_graph : ForeignInGraph model foreign
; foreign_iso : Isomorphism model foreign
}.
```

This provides a link between the `model` type and the `foreign` type, as well as the `graph_predicate` representation of the foreign type and an isomorphism between the two types. This isomorphism is needed for user-level proofs about the behavior of the foreign function, which acts on the foreign type *as if* it were acting on the model type.

The foreign type (such as `C.t`) has a `graph_predicate` that's (typically) a single vertex, in contrast to the graph predicate for the functional model `FM.t` which is (in our example) a Peano chain of unary constructor graph vertices. To connect these, in a way that the Coq type class system can properly instantiate the `foreign_in_graph` component of a `foreign_ann`, we use the following type class:

```
Class ForeignInGraph (model foreign : Type) : Type := model_in_graph : InGraph model.
```

Here, the `model_in_graph` field is the (single-vertex) `graph_predicate` of the foreign (representation) type, masquerading as a `graph_predicate` of the model type; this helps us guide typeclass resolution in the presence of isomorphisms.

The isomorphism class is standard:

```
Class Isomorphism (A B : Type) : Type :=
{ from : A -> B
; to : B -> A
; from_to : forall (x : A), to (from x) = x
; to_from : forall (x : B), from (to x) = x
}.
```


For nonforeign (transparent) types, we define the isomorphism transparently as the identity, so the user can use this fact in Coq correctness proofs. For abstract (opaque) types, we cannot let the user assume that the type is interchangeable with its functional model, only isomorphic:

Definition `transparent` $\{A : \text{Type}\} \text{ } \{IG_A : \text{InGraph } A\} : \text{foreign_ann } A :=$
 $\{ | \text{foreign} := A; \text{foreign_in_graph} := IG_A; \text{foreign_iso} := \text{Isomorphism_refl} | \}.$

Definition `opaque` $\{A B : \text{Type}\} \text{ } \{IG_A : \text{ForeignInGraph } A B\} \text{ } \{Iso : \text{Isomorphism } A B\}$
 $: \text{foreign_ann } A :=$
 $\{ | \text{foreign} := B; \text{foreign_in_graph} := IG_A; \text{foreign_iso} := Iso | \}.$

In practice, we typically instantiate `foreign_iso` with the identity isomorphism, `Isomorphism_refl`. That's because the isomorphism is there more to enforce opaqueness than to relate two different representations. Relating different representations is done in VST funspecs by `graph_predicate` instances, as [section 9](#) will explain.

As we will show, from a `reified` description, we can produce a VST funspec that specifies the correctness of the C function with respect to the functional model (e.g., `FM.add`) operating on the `InGraph` representations. Therefore, every *type Axiom* is justified by an `InGraph` representation predicate, and every *foreign function Axiom* is justified by a VST funspec and proof.

9 A verified foreign function interface

Using these `reified` descriptions of constructor types and of foreign-function types with functional models, VeriFFI sets up the framework for combining C code and Coq code. To relieve the user from boilerplate, it automatically generates the header file `prim.h` (containing C function prototypes) that informs `prim.c` (written by the user, containing C functions).

For each Coq inductive type, VeriFFI generates "glue" operations that allow C code to construct and traverse it. On the verification level, VeriFFI defines predicates for the representation of Coq data types, as well as proofs of general operations on these datatypes. It hence helps the user to preserve an abstraction barrier allowing mostly language-local reasoning.

Primitive functions that do not use the CertiCoq heap—such as `uint63_add`—are straightforward to specify and prove in VST. It is standard in VST (independent of VeriFFI) that the user may supply (for each abstract type) a *representation relation* that relates the functional model of a type (such as Coq `nat`) to its layout in the C program's data-structure memory. In VeriFFI's use of VST, this representation relation takes the form of a custom `graph_predicate` show how, for example, 63-bit integers or packed bytestrings are represented as single vertices in the graph; the purpose of `foreign_in_graph` ([subsection 3](#) is to correctly index Coq's type-class resolution to select that `graph_predicate`.

But VST function-specifications and proofs get more complicated once we have to refer to the CertiCoq heap: we have to ensure that certain invariants are kept. A key contribution of this paper is in both stating these invariants in an abstract way and ensuring that reasoning is independent of the implementation of these invariants.

The conditions of the garbage-collected heap will typically appear as the separation logic predicate `full_gc g t_info roots ti gv`, describing the current state of the data graph `g`, a thread info `t_info`, the roots, the address of the thread info `ti`, and the global variables `gv`. It further comes with a whole list of consistency conditions.

To reason about the graph, we will use propositional⁶ statements on the existence of certain Coq values in the graph; for example, `graph_predicate g n p` states that the natural number `n` is represented in the graph `g` at position `p` : `rep_type`. This `graph_predicate` statement is different

⁶Recall that vertex-in-graph is a "pure propositional" predicate, while graph-in-heap is a separation-logic predicate.

```

Definition uint63_to_nat_spec : ident * funspec :=
  DECLARE _uint63_to_nat
  WITH gv : gvars, g : graph, roots : roots_t, x : {_: FM.t & unit},
        p : rep_type, ti : val, t_info : thread_info
  PRE [ thread_info; int_or_ptr_type ]
        PROP (@graph_predicate FM.t g (projT1 x) p)
        PARAMS (ti, rep_type_val g p)
        GLOBALS (gv)
        SEP (full_gc g t_info roots ti gv; mem_mgr gv)
  POST [ int_or_ptr_type ]
        EX (p' : rep_type) (g' : graph) (roots' : roots_t) (t_info' : thread_info),
        PROP (@graph_predicate nat g' (FM.to_nat (projT1 x)) p';
              gc_graph_iso g roots g' roots';
              frame_shells_eq (ti_frames t_info) (ti_frames t_info'))
        RETURN (rep_type_val g' p')
        SEP (full_gc g' t_info' roots' ti gv; mem_mgr gv).

```

Lemma body_uint63_to_nat : semax_body Vprog Gprog f_uint63_to_nat uint63_to_nat_spec.

Proof. `...` Qed. (* this theorem states that the function body satisfies its spec *)

Fig. 3. Specification and proof of `uint63_to_nat`: Most parts will be identical in any specification interacting with Coq data structures; only the `highlighted parts` are specific to `uint63_to_nat`. The type of `x` in the `WITH` clause (which is isomorphic to `FM.t`) comes from the `args` function’s trivial uncurrying of a 1-argument function. `FM.t` is the dependent product $\{n: \text{nat} \mid n < 2^{63}\}$, so the `PROP` part of the precondition ensures the upper bound on `n`. The `graph_predicate` (at the typeclass instance for `FM.t`) ensures `p` is actually an unboxed integer, i.e., it chooses that constructor of the `rep_type` inductive datatype. Therefore `rep_type_val g p` is a 64-bit integer value. In the postcondition, the `graph_predicate` instance for `nat` ensures that `p'` is a pointer to a Peano natural number in the graph `g'`. (Not shown are two arguments of `full_gc` that are not essential to the explanations in this paper: permission-share for the graph, and an outlier set.)

for each Coq datatype, using type classes that VeriFFI generates automatically as explained in section 4. To be able to use this statement in the presence of garbage collection, it must be invariant under graph isomorphism, so we use the `gc_preserved` component of `InGraph`.

As long as we stay at this abstraction level, the proofs work straightforwardly in VST. For example, the proof of `uint63_to_nat_spec` proceeds by stepping through the propositions while keeping certain invariants about the graph `g` (see subsection 9.2). During each step of the loop, the garbage collector might run, producing new graph `g'`, proved isomorphic to `g` by the specification of the `garbage_collect` function.

9.1 VST function specification

Based on the `reified` description of the type and functional model of `uint63_to_nat`, VeriFFI computes a VST function specification:

Definition `uint63_to_nat_spec` : `ident * funspec` := `fn_desc_to_funspec uint63_to_nat_desc`.

That is, this aspect of glue code generation is not simply a “script” in Python or Ltac, it can be calculated and reasoned about within the logic. With a bit of automatic simplification, this particular `funspec` comes out as shown in Figure 3. As in any VST `funspec`, the `WITH` clause quantifies over all the logical (Coq) variables to be shared between precondition and postcondition. If the caller of this function can find any instantiation of the `WITH` variables for which the precondition is satisfied, then the function will guarantee to satisfy the postcondition with the same instantiation.

In this case, the **WITH** variables are (**gv**) the C program’s static global data addresses; (**g**) the graph; (**roots**) all the pointers in the stack-of-frames, i.e., live local heap-pointer variables of currently stacked function calls; (**x**) the functional model of the input to the function; (**ti**) the pointer to the heap-management data-structure; and (**t_info**) a description of the *contents* of the heap-management data structure.

We choose **C.t** to be equal to **FM.t**; that is, we instantiate **foreign_iso** with the identity isomorphism. The purpose of having an **opaque** isomorphism was just to prevent clients from performing **uint63** operations on **nat** values, or vice versa.

The C function **uint63_to_nat** converts between two very different number representations in the C memory. This difference in representations is manifest in the function-spec by the choice of two different instances of the **InGraph** typeclass, that is, **graph_predicate** instantiations for **FM.t** and **nat** respectively in precondition and postcondition. When these definitions are unfolded, it gives the VST specification of a function that must convert a 63-bit integer (with tag bit) to a chain of Peano **S** constructors.

In detail, this function’s precondition says,

- PRE** [**thread_info**; **int_or_ptr_type**] the C function takes two arguments: a pointer to a thread-info data structure, and a heap-value (a word that may be either an odd integer or a word-aligned pointer).
- PROP**(. . .) the input-argument graph-vertex **p** corresponds to the input functional-model value **x** as described above.
- PARAMS**(**ti**, **rep_type_val g p**) The *values* of the C function parameters are the address of the thread-info struct and the C representation of the graph-vertex **p**. A **rep_type** such as **p** can be one of three things: a boxed vertex in the graph (**repNode v**), an outlier, or an unboxed vertex in the graph (**repZ z**). The function **rep_type_val** translates this representation to a C value; in this case the **graph_predicate** instance in the **PROP** part of the precondition has forced **p** to be a **repZ**, a C integer value.
- SEP**(**full_gc g . . .**, **mem_mgr . . .**) The graph is indeed represented in memory as a separation-logic “resource,” with the garbage-collector’s heap-management data structure. Separately, the malloc/free memory manager (**mem_mgr**) is also in the heap, in case the C program needs to use it for non-Coq data.

The postcondition says,

- POST** [**int_or_ptr_type**] the C function returns a heap-value.
- EX** **p' g' roots' t_info'** there will exist some graph vertex **p'** representing the newly created **nat**, a new graph **g'** (resulting from possibly garbage-collecting the graph **g** as well as adding the new vertex **p'**), and new roots and thread-info (since garbage collection may have forwarded the old roots).
- PROP**(. . .) the new vertex **p'** is the root of a data structure in graph **g'** representing the new **nat**; the new graph **g'** contains an isomorphism of the old graph **g**; and the stack of frames is the same (modulo forwarding of root-pointers by the g.c.).
- RETURN**(**rep_type_val g' p'**) the C function’s return value is the address in memory for graph vertex **p'**.
- SEP**(. . .) the new graph **g'** is represented in memory, along with the representation of the updated g.c. management data **t_info'** and the malloc-free memory manager.

The VST funspec that VeriFFI generates says, “the C function implements its functional model.” You can see the functional model in the **PROP** clause of the postcondition; in this case, it is **FM.to_nat**. That is, the new graph vertex **p'** is supposed to be a representation (in the g.c. graph) of

the functional model applied to the input argument x . (The `projT1` applied to x is an artifact of the degenerate uncurrying of a 1-argument function.)

Most of the predicates used here may be found in any function specification that interacts with CertiCoq/VeriFFI data structures: C globals, a graph, roots of the graph in the C “stack of frames”, permission-share for the heap, the address and contents of the thread-info structure. Whenever we interact with (CertiCoq-compiled) Coq code we require `full_gc`, ensuring wellformedness of the current state. In more detail, `full_gc g t_info roots ti gv` contains

- the spatial representation of the thread-info and the graph;
- C global variables used by the collector;
- several wellformedness and compability conditions on the graph, e.g. that there are no backwards pointers and the graph is coherent with the roots and outliers.

9.2 An example proof

We repeat here from Figure 2 the C implementation of `uint63_to_nat` that constructs a Peano natural number by wrapping n heap-allocated `S` constructors around an `0` constructor:

```
value uint63_to_nat (struct thread_info *tinfo, value t) {
  uint64 i = ((uint64)t)>>(uint64)1; /* strip off the tag */
  value temp = make_nat_0(); /* create the base case */
  while (i) {
    if (tinfo->limit - tinfo->alloc < 2) { /* test whether we need to garbage-collect */
      value roots[1]={temp}; /* register the root-pointer temp */
      struct stack_frame fr = {roots+1,roots,tinfo->fp};
      tinfo->fp= &fr;
      tinfo->nalloc = 2; /* state the need for 2 words */
      garbage_collect(tinfo);
      temp=roots[0]; tinfo->fp=fr.prev; /* fetch temp back and pop the frame stack */
    }
    temp = alloc_make_nat_S(tinfo, temp); /* wrap an S constructor around temp */
    i--;
  }
  return temp;
}
```

The user must then use VST to prove that this C function (whose abstract syntax in Coq we call `f_uint63_to_nat`) satisfies the `uint63_to_nat_spec`—a lemma of the form,

Lemma `body_uint63_to_nat` : `semax_body Vprog Gprog f_uint63_to_nat uint63_to_nat_spec`.

Proof. ... Qed.

Proof. We start by proving that the initial value of `temp` contains a representation in graph g of the natural number 0 , that is, `graph_predicate g 0 p`. Calling `make_nat_0` provides us with a vertex p satisfying this condition. Behind the scenes, p will simply be a leaf in the graph, represented by `repZ`; this information is abstracted from the user.

For the while loop, we require a loop invariant. This one states that there exists $v : \text{rep_type}$, $m : \text{nat}$, $g' : \text{graph}$, thread info t_info' , and a set of $roots'$ such that $m \leq n$, v is the `nat` representation of n in graph g' (`graph_predicate g' m v`), the new graph and forwarded roots are isomorphic to the old graph and original roots (`gc_graph_iso g roots g' roots'`), and all the g.c. invariants hold on the new state (`full_gc g' t_info' roots' ti gv`).

Before the while loop, the loop invariant is easily satisfied by using the postcondition of the first two commands (assigning i and `temp`) and reflexivity of graph isomorphism. Similarly, it is very straightforward in VST to prove that the loop postcondition implies the function postcondition.

In the loop body, we first check whether we still have enough space on the heap and call the garbage collector if we do not. The correctness proof for CertiGC's `garbage_collect` handles, among other things, the stack of root-frames starting at `tinfo->fp` and the establishment of an isomorphic graph `g'` with enough headroom, which still satisfies `full_gc g' t_info' roots' ti gv` and in which constructions that were saved in the roots are preserved. In this case, those constructions include `temp`, which was saved in the topmost frame.

In the loop body after the g.c. test, a new `S` constructor is allocated by calling `alloc_make_nat_S`, whose precondition is that `tinfo->limit - tinfo->alloc ≥ 2`, which has been established by the if-statement. Afterwards, `i` is decreased by 1. The loop invariant is then reestablished, using the postcondition of the funspec for `alloc_make_nat_S` and transitivity of the isomorphism predicate.

VeriFFI Support. To assist with proofs such as the one shown here, VeriFFI provides a library of g.c.-graph isomorphism properties for use in proofs of foreign functions and provides VST-Floyd [Cao et al. 2018] tactical provers for common patterns such as those used here.

Automatically generated glue functions (that construct and traverse Inductive types) are proved fully automatically by a tactic that uses some of the same techniques as shown here. Note that, different to this section, these glue functions go below the abstraction barriers – and hence the proofs have to go below these abstraction barriers and to technical graph manipulations as well: For example, to prove `alloc_make_nat_S` correct, it has to be proven that the newly generated graph still satisfies all the wellformedness conditions in `full_gc g' t_info' roots' bnti gv`.

10 Proving client programs correct using functional models

VeriFFI uses functional models in Coq as specifications of (foreign) functions (operating on foreign abstract types). Recall that the functional model and the actual C representation are connected by isomorphism (section 8). In our example, the functional model of 63-bit int is a range-bounded Peano natural number (a dependent product type), and the functional models of the operations are Coq functions on that type. Proofs of correctness properties of client programs can make use of these functional models. For example, one can easily prove that the prog of Figure 2, which converts 1 and 2 to `C.t`, then adds them, then converts back, results in 3.

Here we show how, using functional models in a client-side proof, one can show that `C.add` is associative:

```

Lemma add_assoc : forall (x y z : nat),
  C.to_nat (C.add (C.from_nat x) (C.add (C.from_nat y) (C.from_nat z))) =
  C.to_nat (C.add (C.add (C.from_nat x) (C.from_nat y)) (C.from_nat z)).
Proof.
  intros x y z.
  (* Step 1: VeriFFI tactic to unpack isomorphisms between C representation and FM *)
  props to_nat_spec. props add_spec. props from_nat_spec. foreign_rewrites.
  (* Proof goal is now,
    FM.to_nat (FM.add (FM.from_nat x) (FM.add (FM.from_nat y) (FM.from_nat z))) =
    FM.to_nat (FM.add (FM.add (FM.from_nat x) (FM.from_nat y)) (FM.from_nat z)) *)
  (* Step 2: an ordinary Coq proof about the functional model *)
  unfold FM.add, FM.from_nat, FM.to_nat.
  unfold proj1_sig.
  rewrite <- !(Nat.Div0.add_mod y z), <- !(Nat.Div0.add_mod x y), <- !(Nat.Div0.add_mod).
  f_equal; apply Nat.add_assoc.
  all: apply Nat.pow_nonzero; auto.
Qed.

```

11 A second example: packed bytestrings

In this section, we give another example of a foreign function that manipulates an abstract type. The Coq `string` type is defined as a list of `ascii`, each of which is record of 8 booleans:

```
Inductive ascii := Ascii : bool->bool->bool->bool->bool->bool->bool->bool->ascii.
Inductive string := EmptyString : string | String : ascii -> string -> string.
```

Each `String` constructor is represented as three 64-bit words (a header and two pointers); each `Ascii` constructor is nine words, in which each boolean is an unboxed constructor, with 1 representing true and 3 representing false. In all, 96 bytes per ASCII character.

As a foreign type with foreign functions, we can provide a packed *bytestring* representation, in which each character occupies one byte, as in OCaml [Minsky and Madhavapeddy 2022, Chapter 23, “string values”]. The header tells the number of 8-byte words, and the last byte of the last word tells how many bytes in that word are meaningful. The special tag 252 indicates that none of the words in the record are pointers—none should be traversed by the garbage collector—so they don’t need to use the last bit of each word to distinguish pointers from integers.



The CertiCoq code generator cannot manipulate the contents of a packed string, because it is not built using ordinary inductive data types. Instead, we can implement it as an abstract datatype, with operations implemented in C and specified using VeriFFI.

11.1 Description of the `pack` function

With the type `bytestring`, the user has chosen a functional model for that type, as a vehicle for describing the functional models of its operations: `FM.bytestring := string`. Now the user provides a Coq type for `pack` : `string -> C.bytestring`, as well as a functional model `FM.pack`. The type of `FM.pack` is completely determined by the type of `pack`, as `string -> FM.bytestring`, which is to say `string -> string`; but what function of that type should it be? Since bytestrings are intended to be an isomorphic (but more efficient) representation of strings, the most straightforward specification choice is the identity function: `FM.pack (x : string) : FM.bytestring := x`. Unlike `C.bytestring` and `C.pack`, which are opaque to the Coq-side client, `FM.bytestring` and `FM.pack` are transparent definitions so the client-side proofs can reason about behavior.

With all these components user-specified, VeriFFI automatically generates the reified description:

```
Definition pack_desc : fn_desc :=
{| type_desc := ARG string _ (fun _ : string => RES FM.bytestring _)
; foreign_fn := C.pack
; model_fn := fun '(s; _) => FM.pack s
; f_arity := 1
; c_name := "pack"
|}.

```

Using VeriFFI’s `args` function (presented in section 5), we can compute the argument type of `pack`. That is, `args pack_desc = {_ : string & unit}`. This is isomorphic to `string`, as we would expect. And therefore, `model_fn pack_desc` (shown as a field of `pack_desc`) simply applies `FM.pack` to its argument, modulo the type isomorphism.

So, the functional model `FM.bytestring` is simply `string`, and the functional model `FM.pack` is simply the identity function. In proofs of the Coq client functions that call `pack` returning results of type `C.bytestring`, one can use the functional model as a reasoning principle by isomorphism between `C.bytestring` and `FM.bytestring`, but the Coq-side client does not know whether type `C.bytestring`

is *equal* to `FM.bytestring` (and hence it cannot possibly know whether `C.pack=FM.pack`). As we will explain, in the VST proofs, we do choose `C.bytestring := FM.bytestring` and `C.pack := FM.pack`.

11.2 Implementation of the `pack` function

We have a hand-written C implementation of the `pack` function that works as follows:

- (1) Traverse the string to calculate its length *len*.
- (2) Test that at least $n = 1 + \lceil (len + 1)/8 \rceil$ words are available in the g.c. “nursery”.
- (3) (If not, save live pointers into the stack-of-frames, call the garbage collector, fetch live pointers from the stack-of-frames.)
- (4) Reserve *n* words of space in the nursery (by adjusting the *heap management data structure*).
- (5) Traverse the string again, translating records-of-8-booleans into bytes, and storing those bytes into the new space.
- (6) Store the header word and trailer bytes (as in the “interface” example).

This function is a bit tricky, because during the traversal at step 5, the heap-management data structure is not coherent with the graph (because one record has been removed from the former but not yet added to the latter). No native Coq function would ever read from the graph during such an incoherence. The proof takes care to accommodate this slightly relaxed invariant.

11.3 Specification of the `pack` function

As usual, VeriFFI computes the VST funspec for `pack` from the `reified` description and functional model, producing something equivalent to the following:

```

Definition pack_spec : ident * funspec :=
  DECLARE _pack
  WITH gv : gvars, g : graph, roots : roots_t, x : {_: string & unit},
        p : rep_type, ti : val, t_info : thread_info
  PRE [ thread_info; int_or_ptr_type ]
      PROP (@graph_predicate string g (projT1 x) p)
      PARAMS (ti, rep_type_val g p)
      GLOBALS (gv)
      SEP (full_gc g t_info roots ti gv; mem_mgr gv)
  POST [ int_or_ptr_type ]
      EX (p' : rep_type) (g' : graph) (roots' : roots_t) (t_info' : thread_info),
        PROP (@graph_predicate bytestring g' (FM.pack (projT1 x)) p';
              gc_graph_iso g roots g' roots';
              frame_shells_eq (ti_frames t_info) (ti_frames t_info'))
        RETURN (rep_type_val g' p')
        SEP (full_gc g' t_info' roots' ti gv; mem_mgr gv).

```

This funspec is much like the one described in subsection 9.1, and only the highlighted parts differ: the abstract type is `bytestring` rather than `C.t`, and the functional model is `string` rather than `nat`. And as in that example, although `bytestring` has a very different representation than `string`, this difference is not reflected in the `foreign_iso` component of the `InGraph` class, which is just an identity isomorphism. The difference in representations is accomplished by using different type-class instances for `graph_predicate` in the precondition (where it is for `string`) and in the postcondition (where it is for `bytestring`). Recall that `graph_predicate` describes how a Coq type is laid out in the graph; the `bytestring` instance uses just a single graph-vertex containing all the bytes of data, whereas the `string` instance uses a chain of `Ascii` constructors. And even though `bytestring` is convertible with `string`, typeclass resolution is by name, not by value.

The user must then use VST to prove that the hand-written C function satisfies `pack_spec`. The proof is hundreds of lines long. The remark above that "this function is a bit tricky" translates to extra work proving that this trickiness is done correctly.

12 Programs with mutation or effects

12.1 Mutable arrays

Purely functional data structures are easier to reason about than imperative data structures. However, they are inherently inefficient for some use cases [Ben-Amram and Galil 1992; Okasaki 1999; Pippenger 1996; Ponder et al. 1988], therefore we inevitably need mutable data structures.

Mutable data structures à la OCaml break purity, which is why we only want to allow them in a controlled way. One way to implement them without breaking purity is to implement them as monadic effects, following the Haskell tradition [Peyton Jones and Wadler 1993; Wadler 1992]. This way, effectful programs are expressed as monadic actions but their effects are not executed until the execution is invoked, which keeps values pure.

A simple monadic interface for a single monomorphic (on element type `elt`) mutable array can be defined as such in Coq:

```
Module Type Array.
  Parameter M : Type -> Type.
  Parameter pure : forall {A : Type}, A -> M A.
  Parameter bind : forall {A B : Type}, M A -> (A -> M B) -> M B.
  Parameter set : nat -> elt -> M unit.
  Parameter get : nat -> M elt.
  Parameter runM : forall {A : Type} (len : nat) (init : elt), M A -> A.
End Array.
```

Here we have a monad type, followed by return and bind functions for monadic values. We also have operations for assigning a value to an index in the array, and getting the value at an index in the array. Finally, we have a `runM` function, which takes the length of the array and a default value for undefined indices, executes a monadic action, and returns the final result. The `runM` function has local mutation but is externally pure; a client of `runM` cannot tell if it has local mutation inside.⁷

C implementation. We define a Coq module for the foreign types and functions for mutable arrays:

```
Module C <: Array.
  Inductive M : Type -> Type :=
  | pure : forall {A : Type}, A -> M A
  | bind : forall {A B : Type}, M A -> (A -> M B) -> M B
  | set : nat -> elt -> M unit
  | get : nat -> M elt.

  Axiom runM : forall A (len : nat) (init : elt), M A -> A.
End C.
```

⁷Launchbury and Peyton Jones [1994], in their presentations of the `ST` monad in Haskell, also achieve the local mutation and external purity but for a more versatile interface that allows creating multiple mutable references in the same monad. In their approach, a clever trick based on rank-2 types forbids mutable references to escape the monad. In our approach, we never expose the mutable reference as our monad only operates on one monad. Our approach is more similar to that of Sakaguchi [2020], but we forgo the intrinsic guarantees about indices for the sake of simplicity and use a default element instead.

We implement operations in the mutable array monad as a free monad with extra constructors for the operations.⁸ The only foreign function in this module that will be backed by a C implementation is `runM`.

We will elide the full C implementation of `runM` here, although we will provide an explanation in prose. In the C implementation of `runM`, we create a block in the CertiCoq heap with the length `len`, traverse the monadic action of the inductive type `C.M`, and return the result. When we see a `set` action, we want to find the right slot in the array and assign the new value in that slot. However, we have to notify the garbage collector when we update a mutable reference, because the generational garbage collector operates on the assumption that older records never point to newer records, unless the addresses of those references are recorded in a *remembered set* [Lieberman and Hewitt 1983].

A functional model and correctness. As in subsection 3.2, we will define a functional model for mutable arrays and discuss how its C implementation and its client programs can be verified.

Following the Haskell tradition [Peyton Jones and Wadler 1993], we define the functional model of the monad `M` as a function from the state to a pair of a result and the new state. In the state, we model the array with a linked list, and `get/set` the element at a particular index functionally.

Given that the only foreign function in the `C` module is `C.runM`, we only have to generate and prove a VST spec about `C.runM`. There is nothing particularly special about `C.runM`, we can generate a `fn_desc` for it, compute a VST spec using `fn_desc_to_funspec`, and attempt to prove it correct. However, we have not yet done the VST proof that the C function satisfies this `funspec`.

In section 10 we proved properties about client Coq programs of integers, now we want to do the same for client Coq programs of mutable arrays. In the example below, we prove that first `setting` an index of an array to a value and then `getting` the value at that index, gives the same final result (but not the same state). Our proof once again resembles that of Swierstra and Altenkirch [2007], since we use the functional semantics in our functional model to reason about mutable state:

```

Lemma set_get :
  forall (n len : nat) (bound : n < len) (init : elt) (to_set : elt),
    (C.runM len init (C.bind (C.set n to_set) (fun _ => C.get n)))
  = (C.runM len init (C.pure to_set)).
Proof.
  intros n len bound init to_set.
  (* Step 1: VeriFFI tactic to unpack isomorphisms between C representation and FM *)
  props runM_spec. foreign_rewrites.
  props bind_spec. props pure_spec. foreign_rewrites.
  props set_spec. props get_spec. foreign_rewrites.
  (* Proof goal is now,
    (FM.runM len init (FM.bind (FM.set n to_set) (fun _ => FM.get n)))
    = (FM.runM len init (FM.pure to_set)) *)
  (* Step 2: an ordinary Coq proof about the functional model *)
  ...
Qed.

```

12.2 Programs with input/output

We can use the same free monad idea for expressing effectful programs. For instance, we can extend the bytestring example with an effectful interface to print bytestrings from `stdout` and

⁸Technically, Coq's module system does not allow inductive types and their constructors to act as fields outlined by a **Module Type**. In the actual implementation, we declare the inductive type and its constructors with different names and later create aliases.

read bytestrings from `stdin`. We will follow the same recipe: first define a **Module Type** that has a monadic type and monadic actions, then define a `C` module that has an inductive type to represent the free monad.

We diverge from that recipe here, as we cannot have an equivalent of `runM` for this monad—as our monadic actions here depend on the real world and therefore are not pure. Each call to `runM` would have to create a different “outside world” to interact with. Therefore, we will not expose `runM` to the Coq side. We will implement it in `C`, and we will call it only once from the `C` side. Since there is no Coq reference to `runM`, we will have to write the VST specification of it by hand. Writing this specification and proving it requires dealing with side effects using VST, which is quite capable of accommodating proofs about effectful `C` programs. We leave the VST specification and proof of `runM` as future work.

This choice also affects how we prove properties about client programs. When we stated the `set_get` lemma about mutable arrays, we claimed the equivalence of two monadic actions, by calling `C.runM` on both of those programs, then asserting that they were equal using Coq’s standard equality `=`. However, there is no `runM` function for the effectful monadic actions. To state the equivalence of monadic actions in the absence of `runM`, we define our own relation that states the equivalence of two monadic programs. We need the new relation to exist both in the `C` module and `FM` module in Coq, therefore it makes sense to add it to the interface. We add

```
Parameter same_behavior : forall {A : Type}, M A -> M A -> Prop.
```

to the **Module Type** we define for bytestrings. While we do not need to provide a `C` implementation for this function, we will have an **Axiom** for it in the `C` module and a functional model definition for it in the `FM` module. We can then state the equivalence of two monadic programs using this relation. Here we state that a program that prints two bytestrings sequentially behaves the same as a program that appends those two bytestrings and prints it once:

```
Lemma print_steps :
  forall (a b : C.bytestring),
    C.same_behavior (C.bind (C.print a) (fun _ => C.print b))
      (C.print (C.append a b)).
```

In the proof of this lemma, we can rewrite the calls to the components from the `C` module to their counterparts in the `FM` module. Once we get to a proof goal entirely about the functional model, we can proceed with the proof as if it is about a purely functional program.

Although we present a simple, inductive interface in this section for presentation purposes, we believe our system can express other styles of monadic interfaces described in the literature. `FreeSpec` [Latan et al. 2021] allows effects to be represented modularly, while interaction trees [Xia et al. 2019] allow reasoning about possibly nonterminating effectful programs through a coinductive interface. Nigron and Dagand [2021] and Carnier et al. [2024] pave an alternative path for reasoning about effects, in which custom monads get domain-specific reasoning with custom program logics.

13 Soundness

Assuming that the `CertiCoq` compiler is correct, then the `VeriFFI` system is sound. In this section we explain the basis for that claim, and how (in future work) it could be proved.

We rely primarily on the verified-in-Coq soundness of the Verified Software Toolchain [Appel et al. 2014]. Here we explain the VST soundness theorem informally. Suppose one has a set of functions named i_0, i_1, \dots, i_{n-1} with function-bodies (including headers) f_0, \dots, f_{n-1} and funspecs s_0, \dots, s_{n-1} . We collect the funspecs into a *context* $\Gamma = [(i_0, s_0); \dots; (i_{n-1}, s_{n-1})]$. Suppose we prove the correctness of each function individually:

$$\text{semax_body } \Gamma \ f_j \ (i_j, s_j) \quad \text{that is,} \quad \Gamma \vdash \{\text{pre}(s_j)\} f_j \{\text{post}(s_j)\}$$

such as the lemma `body_pack` mentioned in [subsection 9.2](#). Whenever a function-body f_j calls some function named i_k , the correctness proof can assume the specification (i_k, s_k) for that function found in assumption Γ (even if $j = k$, i.e., recursion is supported by VST’s step-indexed semantic model). Suppose the initial state when calling function f_0 satisfies the precondition $\text{pre}(s_0)$. **Then** executing function f_0 in the operational semantics of CompCert C will not crash, and if it terminates, the resulting state will satisfy the postcondition $\text{post}(s_0)$. VST is a logic of partial correctness, and does not prove termination—this is a limitation of higher-order impredicate program logics based on step-indexed models (such as VST and Iris [[Jung et al. 2018](#)]), but in return one gets powerful reasoning about pointers, function-pointers, and recursion.

When using VeriFFI, we have:

- The top-level Coq function g_0 that has internal functions g_{n+1}, \dots, g_{n+m} , all of which are clients of foreign functions named i_1, \dots, i_n ; that is, the i_1, \dots, i_n are free variables of g_0 . Function g_0 is compiled by CertiCoq into a C function f_0 with auxiliary functions $f_{n+1}, \dots, f_{n+m'}$, which are not internal to f_0 because they have been hoisted to top level after closure conversion; and m' may differ from m because of optimizations and transformations by the CertiCoq compiler.
- C functions f_1, \dots, f_n with names i_1, \dots, i_n . These functions have functional models g_1, \dots, g_n from which VeriFFI automatically generates funspecs s_1, \dots, s_n as described in [subsection 9.1](#).
- One `garbage_collect` function written in C, and the auxiliary functions it calls.

We generate the funspecs of the f_1, \dots, f_n from their functional models g_1, \dots, g_n , using `fn_desc_to_funspec` (for user-written C functions) or in a related way for glue-code-generated C functions that allocate data constructors. We generate a funspec s_0 from function g_0 using `fn_desc_to_funspec`. We do not need funspecs for f_{n+1}, \dots, f_{n+m} because the proof of correctness of CertiCoq relates those functions to f_0 using direct operational-semantic methods.

From the CertiCoq compiler-correctness claim, we hypothesize, `semax_body` $\Gamma f_0 (i_0, s_0)$. The CertiCoq team has not yet completed this correctness proof: the entire front-end is proved correct in Coq [[Sozeau et al. 2019](#)], the entire λ ANF back-end is proved correct in Coq [[Paraskevopoulou 2020](#); [Paraskevopoulou et al. 2021](#)], the code generator is proved correct, but the composed end-to-end theorem is still under construction.

In fact, CertiCoq’s end-to-end compiler correctness theorem *for open programs (i.e., with foreign functions as free variables)*, has not yet even been stated. Our work here provides the framework for doing so, and suggests that the proof should follow VST’s semantic method for stapling together a collection of `semax_body` proofs of mutually recursive higher-order functions. That is, the CertiCoq theorem should relate the Coq function g_0 to the operational behavior of the generated code f_0 , subject to assumptions about the operational behavior of the N primops. We can talk about operational behavior in this way because VST’s `semax_body` predicate is a shallow-embedded definition stating properties of a CompCert Clight operational-semantic execution—not, for example, an inductive definition which could only be proved by a certain set of Hoare-logic proof rules.

Now, for every one of these functions we need a `semax_body` proof of its correctness w.r.t. its funspec.

- The `garbage_collect` function was proved correct by [Wang et al. \[2019\]](#) using VST.
- The proof of `semax_body` $\Gamma f_0 (i_0, s_0)$, relying on related proofs for $f_{n+1}, \dots, f_{n+m'}$, will be a consequence of CertiCoq compiler correctness, as described above.
- The `semax_body` proofs of f_1, \dots, f_n are done using the Verified Software Toolchain’s VST-Floyd proof automation system. For those of the f_j that allocate or discriminate data constructors, whose C functions were generated fully automatically by VeriFFI glue code, VeriFFI generates these VST-Floyd proofs automatically using an Ltac script. For the f_j functions whose C

functions are written by hand by the user, the VST-Floyd proofs are done interactively by the user, with assistance from VST-Floyd.

All these `semex_body` proofs can be tied together using VST’s `semex_func` constructor lemmas [Appel et al. 2014, page 207] into a single program-correctness proof.

Total correctness vs. partial correctness. The source function g_0 provably terminates (because it type-checks in Coq); and the functional models g_1, \dots, g_n are total functions (because they are expressed as functions in Coq). However, the VeriFFI+CertiCoq proof of the whole program will not guarantee termination, because VST’s program logic is a Separation Hoare logic of partial correctness. This is not a defect of VeriFFI; it is inherent in compiling Coq to any computer architecture with a fixed number of address bits (e.g., 64-bit addresses). The Coq function that computes Ackermann’s function on Peano natural numbers is a total function, but compiled to RISC-V it will inevitably run out of memory even on smallish inputs.

14 Related work

14.1 Verified FFI systems

Melocoton [Guéneau et al. 2023] allows users to write programs in a toy subset of OCaml and a toy subset of C and reason about both sides and their interactions. Users can verify their OCaml code in an OCaml program logic, and their C code in a C program logic, where both program logics are defined on top of Iris, a separation logic framework embedded in Coq. Following the conventional way of verifying interoperability through a combination of languages [Matthews and Findler 2007; Perconti and Ahmed 2014], Melocoton defines operational semantics and program logics for C, OCaml, and their combination, a “multi-language semantics”. The user does not have to interact with the combined language and its program logic, but the combined program logic is essential to tie the separate parts together. Melocoton does not include a verified garbage collector, but it has reasoning based on a nondeterministic model of a garbage collector.

In contrast to Melocoton, VeriFFI allows users to write programs in all of Gallina and almost all of C. The user can reason about their Coq programs directly in Coq, which is already a logic and proof assistant and therefore easier to reason in, and about their C programs in Coq via the Verified Software Toolchain [Cao et al. 2018], a separation logic framework embedded in Coq.

For VeriFFI we did not have to develop a combined language and a combined program logic for two languages; it has a simpler architecture than Melocoton because of the languages it is based on: Coq is both our language of reasoning, and the source and implementation language of our compiler. On the other end of the spectrum, C is both the target language of our compiler and the language of our foreign functions. This coincidence means our multi-language programs can just be “plugged together,” as both the compiler output of our Coq code and our foreign functions are in C. Hence, all of our reasoning about foreign functions can be achieved within the Verifiable C program logic. VeriFFI is also based on a verified garbage collector, CertiGC, whose heap graph representation is essential in how VeriFFI reasons about the representation of Coq values in memory, and whose implementation can be linked to compiled to Coq programs.

Cogent [Cheung et al. 2022] allows one to write functional programs in the HOL logic, that type-check in HOL and can be proved correct in HOL; but that *also* type-check in a much more restrictive first-order linear type system—that is, no nested higher-order functions, no sharing of data structures. These first-order linear programs are compiled to C code that (because linear) can use `malloc/free`, and do not require a garbage collector. Although that is a reasonable trade-off to make, it severely restricts the expressiveness of the functional language.

CakeML [Kumar et al. 2014] is a compiler for a subset of Standard ML, verified in the HOL4 proof assistant. Guéneau et al. [2017] integrate Characteristic Formulae, a separation logic for stateful

ML programs, into CakeML. This system supports foreign functions as well, but ultimately this system reasons about ML, the higher-level side of the two languages interacting via the FFI. Hence, it is possible to write specifications on how the foreign function is used in ML, but there is no mechanism to verify that the foreign function is implemented correctly. In comparison, VeriFFI allows both reasoning about the higher-level side, since it is just Coq code, and the lower-level side, since VST's separation logic and C program logic is available.

Æuf [Mullen et al. 2018] is another verified compiler project from Coq to C. *Æuf* can compile a subset of Gallina, with no user-defined types, dependent types, fixpoints, or pattern matching. In comparison, CertiCoq can compile all of Gallina. *Æuf*'s compiler correctness theorem allows the shim (wrapper code in C that executes the compiled Coq program) to be verified using VST, but it does not have a story about how Coq programs can call C programs, or regarding the specified/verified attachment of a garbage collector.

14.2 Other compilers and FFI systems

Foreign function interfaces achieve interoperability by having one language mimic the calling conventions of the other language [Matthews 2008]. For FFI systems where the lower-level language is C, having C types exposed to the higher-level language is common. While exposing base C types like `int`, `void`, and pointers suffices for most cases, it is possible to encode more complicated C types such as `structs` and `unions` into the higher-level language. Blume [2001] presents an example of this for Standard ML and Yallop et al. [2018] demonstrate a different design for OCaml. In these approaches, the glue code generators catch discrepancies between the types of foreign functions and their higher-level representations. VeriFFI does not expose the C types to Coq, but it would be possible to implement a library that does so, and prove properties about it.

Some FFI systems expose the value representation of the higher-level language to the lower-level language. OCaml's values are represented in C with the `value` type [Leroy 1999], which CertiCoq and VeriFFI reuse. Similarly, Java's JNI [Liang 1999] achieves interoperability by exposing the higher-level language's values to the lower-level language, where the user has access to C types such as `jstring` and `jobject` for Java strings and objects.

Furr and Foster [2005] explore static checks to ensure that foreign functions do not violate type safety in OCaml, and in later work, Java's JNI [Furr and Foster 2006, 2008]. Their work involves automatic inference of higher-level language types from foreign function implementations in C, and therefore is easier than VeriFFI to apply in larger codebases. In comparison, VeriFFI guarantees type safety as a corollary of correctness. In a similar line of work, Tan et al. [2006] add static and dynamic checks to ensure that foreign code does not violate memory safety or Java's type safety.

Löw et al. [2019] describe verified system calls for CakeML, but they make no claim regarding support for data structures, inductive data types, glue code generation, representation predicates, or a program logic for proving correctness of their foreign functions.

VeriFFI can be used to implement particular data types more efficiently and bring compiler optimizations on a case-by-case basis to CertiCoq compiled code. For example, Baudon et al. [2023] and Elsmann [2024] present a technique called "bit-stealing" to represent algebraic data types using less space, and implement a compiler that uses this technique in all data types. While CertiCoq does not use this technique in its representation of Coq values, it is possible to implement a foreign type that makes this optimization for a particular type, and prove it correct using VeriFFI. One useful example would be an integer type that has one constructor that carries a 63-bit integer and another constructor that carries a big integer. Since constructor payloads differ in their boxities, we do not need boxed constructors and constructor headers to distinguish between the machine and big integers.

15 Future work

Proofs about programs with mutation and input/output. Our mutable array monad is implemented as described in [subsection 12.1](#), our glue code generator supports working interoperation of the Coq and C sides, and VeriFFI generates appropriate VST funspecs. In future work we will complete the VST proof of this monad’s `runM` function. Our input/output monad is implemented as described in [subsection 12.2](#), but the VST specification for its `runM` function (unexposed to Coq to keep purity) cannot be generated. In future work we will state the VST specification for this C function, and complete the VST proof.

Persistent, internally mutable data structures. In a functional language one can have “persistent” data structures that present a purely functional interface but mutate themselves internally for efficiency [[Conchon and Filliâtre 2007](#), §2.3]. It may be possible to support this by writing a `graph_predicate` that permits multiple graph representations of the same Coq value.

End-to-end soundness. We plan to work with the CertiCoq team to specify and verify the correctness of *open* Coq expressions, that is, programs that call external functions—following the methodology explained in [section 13](#). Based on that—using the VST semantic model of the function specification in terms of the Clight operational semantics—it should be straightforward to build a machine-checked proof of soundness for VeriFFI.

Retargeting. The Coq formalizations described in [sections 4, 5, 6, and 8](#) are entirely independent of the target language, so this work could be retargeted to CertiCoq’s WebAssembly back end [[Meier et al. 2024](#)].

16 Conclusion

For a (dependently) typed functional language to interact with a low-level language, at least one language must be taught how to traverse the data structures of the other, and master the calling conventions of the other; and, for verification, to *reason* over the gap. Our glue code generator allows C to traverse (and build) Coq data structures; allows C functions to support Coq calling conventions; and allows C functions to be proved correct with respect to Coq functional models. Our program logics on both sides are very rich and expressive: Coq (the CiC logic) is a widely used and well-established logic for reasoning about functional programs written in that logic; our system for specifying and verifying across interfaces permits both concrete data types (C traversal/construction of Coq inductive constructors) and abstract data types (C representations unachievable in pure Coq).

Proofs in VST that foreign functions satisfy their funspecs are often long and tedious. If only there were a way to automatically synthesize proofs of C functions from their Coq functional models! But there *is* such a way: it’s called CertiCoq, which compiles Coq functions into certified-correct C code. This is the right way to do it for most functions. But for functions (such as `pack`) operating on data types whose representations cannot be described efficiently by Coq constructors, or whose algorithms cannot be efficient enough as functional programs on such constructors, we need a way to write highly tuned C programs by hand and prove them correct using VST’s powerful program logic. And that way is VeriFFI, the Verified Foreign Function Interface.

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